32.48. Model: The magnetic field is that of two long wires that carry current. Visualize:

Solve: (a) For x > +2 cm and for x < -2 cm, the magnetic fields due to the currents in the two wires add. The point where the two magnetic fields cancel lies on the *x*-axis in between the two wires. Let that point be a distance *x* away from the origin. Because the magnetic field of a long wire is $B = \mu_0 I/2\pi r$, we have

$$\frac{\mu_0}{2\pi} \frac{(5.0 \text{ A})}{(0.02 \text{ m} + x)} = \frac{\mu_0}{2\pi} \frac{(3.0 \text{ A})}{(0.02 \text{ m} - x)} \Rightarrow 5(0.02 \text{ m} - x) = 3(0.02 \text{ m} + x) \Rightarrow x = 0.005 \text{ m} = 0.50 \text{ cm}$$

(b) The magnetic fields due to the currents in the two wires add in the region -2.0 cm < x < 2.0 cm. For x < -2.0 cm, the magnetic fields subtract, but the field due to the 5.0 A current is always larger than the field due to the 3.0 A current. However, for x > 2.0 m, the two fields will cancel at a point on the *x*-axis. Let that point be a distance *x* away from the origin, so

$$\frac{\mu_0}{2\pi} \frac{5.0 \text{ A}}{x + 0.02 \text{ m}} = \frac{\mu_0}{2\pi} \frac{3.0 \text{ A}}{x - 0.02 \text{ m}} \Rightarrow 5(x - 0.02 \text{ m}) = 3(x + 0.02 \text{ m}) \Rightarrow x = 8.0 \text{ cm}$$